



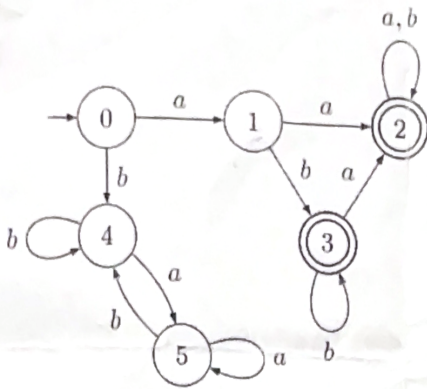
**VIT**  
Vellore Institute of Technology  
(Deemed to be University under section 3 of UGA, Act, 1956)

Continuous Assessment Test- 1(CAT-1)- September 2022

|              |                                                                                                                                                      |              |                                                                                                                                           |
|--------------|------------------------------------------------------------------------------------------------------------------------------------------------------|--------------|-------------------------------------------------------------------------------------------------------------------------------------------|
| Programme    | : B.Tech. [CSE and Specialization]                                                                                                                   | Semester     | : FS 22-23                                                                                                                                |
| Course Code  | : BCSE304L                                                                                                                                           | Slot         | : B2+TB2                                                                                                                                  |
| Course Title | : Theory of Computation                                                                                                                              |              |                                                                                                                                           |
| Faculty(s)   | : Dr. Prakash P,<br>Dr. Smrithy G S,<br>Dr. Sivakumar,<br>Dr. Ashoka Rajan R,<br>Dr. B V A N S S Prabhakar Rao,<br>Dr. Sureshkumar,<br>Dr. Maria Anu | Class Nbr(s) | : CH2022231001522,<br>CH2022231001523,<br>CH2022231001524,<br>CH2022231001525,<br>CH2022231001528,<br>CH2022231001530,<br>CH2022231001532 |
| Time         | : 90 Minutes                                                                                                                                         | Max. Marks   | : 50                                                                                                                                      |

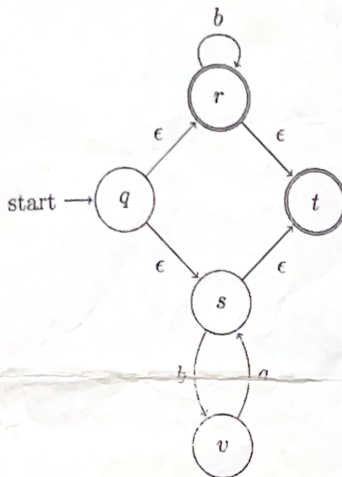
Answer ALL the Questions

| Q.No. | Sub. Sec. | Questions                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | Marks |
|-------|-----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|
| 1.    |           | <p>Consider the following two languages:<br/><math>L_1 = \{aa, bb\}</math> where <math>\Sigma = \{a, b\}</math><br/><math>L_2 = \{ppp, qqq\}</math> where <math>\Sigma = \{p, q\}</math>.</p> <p>Compute the following:</p> <p>a) <math>L_3 = (L_1)^2 \cdot L_2</math><br/>b) <math>L_4 = L_2 \cdot \epsilon</math><br/>c) <math>L_5 = L_2 - L_3</math><br/>d) <math>L_6 = L_2 \cap L_4</math><br/>e) <math>L_7 = (L_5)^*</math></p> <p><i>Handwritten: {aaaaa bbbbbb}</i></p> | 2*5   |
| 2.    | a.        | Design a deterministic finite automaton to accept,<br>$L = \{w \in \{a,b\}^* \mid n_a(w) \bmod 3 \geq n_b(w) \bmod 2\}$<br>where $n_a$ and $n_b$ represents the number of a's and number of b's, respectively.                                                                                                                                                                                                                                                                 | 7     |
|       | b.        | Check whether the string "aabbbb" is accepted by L or not. Justify your answer.                                                                                                                                                                                                                                                                                                                                                                                                | 3     |
|       |           | Construct a minimized deterministic finite automaton for the automaton given below.                                                                                                                                                                                                                                                                                                                                                                                            | 10    |



Convert an equivalent deterministic finite automaton for the automaton given below.

10



5. a. Construct a NFA over  $\Sigma = \{a, b, c\}$  to accept the language,  
 $L = \{w \mid w \in \Sigma^* \text{ contain some characters in } \Sigma \text{ that appears at most twice in } w\}$ .
- b. Construct a finite automaton to accept the language,  
 $L = \{w \in \{a, b\}^* \mid \text{contain strings where } |w| \bmod 2 = 1 \text{ or } |w| \bmod 3 = 2 \text{ or } |w| \bmod 4 = 3\}$   
 [Hint:  $|w|$  represents the length of the string  $w$ ]

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